

# **MATHEMATICS APPLICATIONS**

## **MAWA Semester 2 (Units 3 & 4) Examination 2017**

**Calculator-free**

**Marking Key**

**Section One: Calculator-free**

**(50 Marks)**

**Question 1 (a)**

Solution	
$T_2 = 2, T_3 = 0.5 \times 2 - 8 = -7$	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies second term</li> </ul>	1
<ul style="list-style-type: none"> <li>determines an expression for the third term</li> </ul>	1
<ul style="list-style-type: none"> <li>calculates third term</li> </ul>	1

**Question 1 (b)**

Solution	
$T_n = -4n + 9, n = 50$	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>deduces and expression for the nth term</li> </ul>	1
<ul style="list-style-type: none"> <li>determines <math>-4n = -200</math></li> </ul>	1
<ul style="list-style-type: none"> <li>determines <math>n = 50</math></li> </ul>	1

**Question 2 (a)**

Solution	
Each edge represents a connection between stations	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies representation of an edge</li> </ul>	1

**Question 2 (b)**

Solution	
CMEKPNRZWHT or CHTRZWEMNPK	
Marking key/mathematical behaviours	Marks
Identifies a route which	
<ul style="list-style-type: none"> <li>starts at C and ends at a different node</li> </ul>	1
<ul style="list-style-type: none"> <li>travels through each node once only</li> </ul>	1
<ul style="list-style-type: none"> <li>has no repeated edges</li> </ul>	1

**Question 2 (c)**

Solution	
The graph can be drawn in 2 dimensions without any edges crossing	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>describes planarity</li> </ul>	1

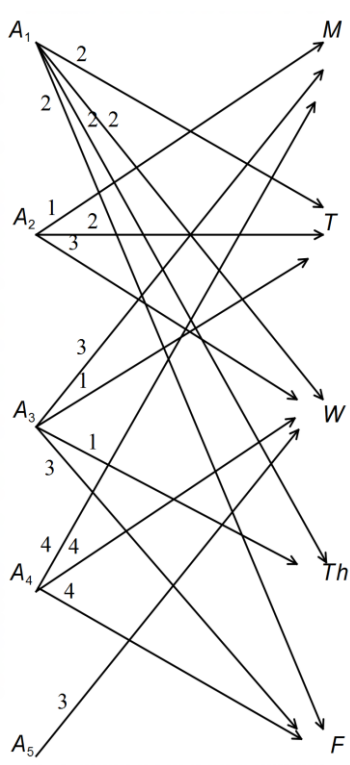
**Question 2 (d)**

Solution	
$v = 11, f = 11, e = 20.$	
$v + f - e = 2$	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>determines values for the numbers of faces, edges and vertices</li> </ul>	1
<ul style="list-style-type: none"> <li>expresses the relationship between <math>e, f</math> and <math>v</math></li> </ul>	1

**Question 2 (e)**

Solution	
(i) Louise would need to come back through R or H to reach T and Z and one of the conditions is to visit each station only once.	
(ii) NEM, NEW	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>describes inability to meet a necessary condition</li> </ul>	1
<ul style="list-style-type: none"> <li>identifies alternate incorrect starting route</li> </ul>	1

**Question 3 (a)**

Solution	
	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>10 edges correctly weighted</li> </ul>	1
<ul style="list-style-type: none"> <li>15 edges correctly weighted</li> </ul>	1
<ul style="list-style-type: none"> <li>10 edges correctly positioned</li> </ul>	1
<ul style="list-style-type: none"> <li>15 edges correctly positioned</li> </ul>	1

**Question 3 (b)**

Solution

$$\begin{bmatrix} 3 & 0 & 4 & 0 \\ 1 & 2 & 3 & 2 \\ 4 & 3 & 4 & 5 \\ 5 & 2 & 1 & 2 \end{bmatrix} \dashrightarrow \begin{bmatrix} 2 & 5 & 1 & 5 \\ 4 & 3 & 2 & 3 \\ 1 & 2 & 1 & 0 \\ 0 & 3 & 4 & 3 \end{bmatrix} \dashrightarrow \begin{bmatrix} 1 & 4 & 0 & 4 \\ 2 & 1 & 0 & 1 \\ 1 & 2 & 1 & 0 \\ 0 & 3 & 4 & 3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3 & \textcircled{0} & 4 \\ 2 & \textcircled{0} & 0 & 1 \\ 1 & 1 & 1 & \textcircled{0} \\ \textcircled{0} & 2 & 4 & 3 \end{bmatrix}$$

Maximum number of hours is 16

V<sub>1</sub> comes on Wednesday

V<sub>2</sub> comes on Tuesday

V<sub>3</sub> comes on Thursday

V<sub>4</sub> comes on Monday

Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>subtracts every number from the maximum number</li> </ul>	1
<ul style="list-style-type: none"> <li>reduces two rows</li> </ul>	1
<ul style="list-style-type: none"> <li>reduces further two rows</li> </ul>	1
<ul style="list-style-type: none"> <li>identifies maximum number of hours</li> </ul>	1
<ul style="list-style-type: none"> <li>describes allocation of volunteers</li> </ul>	1

**Question 4 (a)**

Solution

B. The weekly allowance is \$1100 whereas it is \$1000 in both A and C.

Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies correct rule</li> </ul>	1
<ul style="list-style-type: none"> <li>explains choice of rule</li> </ul>	1

**Question 4 (b)**

Solution

C. 1.10 as the ratio represents 110% so a 10% increase each year.

Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies correct rule</li> </ul>	1
<ul style="list-style-type: none"> <li>explains choice of rule</li> </ul>	1

**Question 4 (c)**

Solution	
$\begin{aligned} \text{Amount} &= 1.05 \times 500\,000 - 1000 \times 52 \\ &= 500\,000 + 25\,000 - 52\,000 \\ &= \$473\,000 \end{aligned}$	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>determines 5% of 500 000</li> <li>calculates value after one year</li> </ul>	1
	1

**Question 4 (d)**

Solution	
<p>Rule C</p> <p>The payout is the same each year as A but the rate of growth is higher than in A. In B the growth is 8% per year which is lower than in C and the payout is higher by \$100. This mean the investment is growing at a slower rate and reducing by more money each year.</p>	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>compares the influence of the rates for A, B, C</li> <li>identifies the significance of the different amounts transferred</li> <li>concludes that C is the best option</li> </ul>	1
	1
	1

**Question 5 (a)**

Solution	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>plots and labels A</li> <li>plots and labels B</li> </ul>	1
	1

**Question 5 (b)**

Solution	
Number of attempts	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies explanatory variable</li> </ul>	1

**Question 5 (c)(i)(ii)**

Solution	
(i) You cannot get a success of 2.3 with 0 attempts because there are no successes possible OR a success cannot be fractional.	
(ii) 5. The rate is 0.5 successes per attempt and 0.5 of 10 is 5	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>interprets the vertical intercept</li> </ul>	1
<ul style="list-style-type: none"> <li>determines change in the number of successes</li> </ul>	1
<ul style="list-style-type: none"> <li>interprets the gradient</li> </ul>	1

**Question 5 (d)**

Solution	
ABOVE	
For the same number of attempts their number of successes is greater so they would be above the same number of attempts as a less successful player	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>interprets scatter plot</li> </ul>	1
<ul style="list-style-type: none"> <li>explains positioning on scatter plot</li> </ul>	1

**Question 5 (e)**

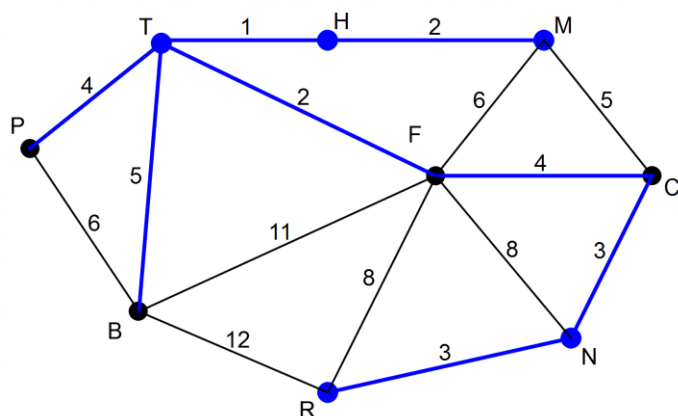
Solution	
INCREASE	
There is less variation as only the least successful players are left	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>concludes a lower correlation coefficient</li> </ul>	1
<ul style="list-style-type: none"> <li>explains the lower correlation coefficient</li> </ul>	1

**Question 5 (f)**

Solution	
C	
Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies most likely residual plot</li> </ul>	1

Question 6 (a)

Solution



24 km

Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies 8 correct roads and not incorrect roads</li> </ul>	1
<ul style="list-style-type: none"> <li>identifies a further 2 correct roads without any incorrect roads</li> </ul>	1
<ul style="list-style-type: none"> <li>determines length of cycle paths</li> </ul>	1

Question 6 (b)

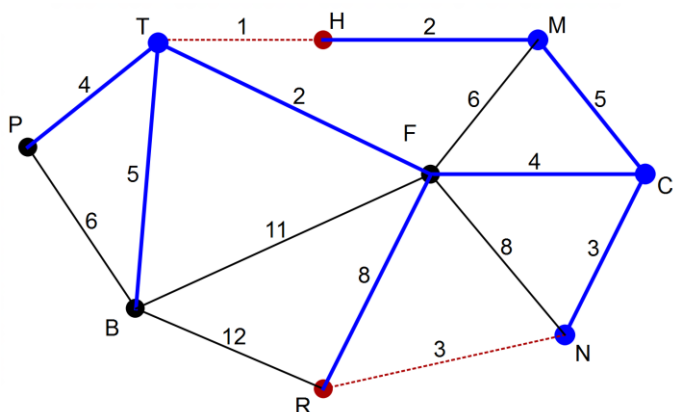
Solution

PB, BR, BF, RF, FB, FN, BC

Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies all roads not required</li> </ul>	1

Question 6 (c)

Solution



Cycle paths are now 33 km  
MC and FR are now needed

Marking key/mathematical behaviours	Marks
<ul style="list-style-type: none"> <li>identifies change in length</li> </ul>	1
<ul style="list-style-type: none"> <li>identifies change of edges</li> </ul>	1